# ÉCOle polytechnique fédérale de lausanne 

School of Computer and Communication Sciences

Problem 1. Consider the three probabilitiy distributions $R=\{0.25,0.25,0.25,0.25\}, P=$ $\{0.4,0.35,0.15,0.1\}$ and $Q=\{0.25,0.35,0.15,0.25\}$.

1. Compute the three entropies $H(R), H(P)$ and $H(Q)$. Which one is larger?
2. Can you answer the above question without computing explicitly $H(R), H(P)$ and $H(Q)$ ?

Problem 2. Consider a random variable $s$ which takes an infinite number of values whith corresponding probabilities $p_{i}=\frac{\alpha}{2^{2+1}}, i \in \mathbb{N}=\{1,2,3, \ldots\}$.

1. For what value of $\alpha$ this is a probability distribution?
2. What is the entropy of $s$ ?

Hint: If $|r|<1, \sum_{i=0}^{\infty}(a+i d) r^{i}=\frac{a}{1-r}+\frac{r d}{(1-r)^{2}}$.
Problem 3. For each of the following three codes, say if it is uniquely decodable. If so, is it instantaneous?

|  | Code 1 | Code 2 | Code 3 |
| :--- | ---: | ---: | ---: |
| $s_{1}$ | 0 | 0 | 0 |
| $s_{2}$ | 1 | 10 | 01 |
| $s_{3}$ | 00 | 110 | 011 |
| $s_{4}$ | 11 | 111 | 111 |

